

Smales problem for critical points on certain two rays

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Abstract

Let f be a polynomial of degree $n \geq 2$ with $f(0) = 0$ and $f'(0) = 1$. We prove that there is a critical point ζ of f with $|f(\zeta)/\zeta| \leq 1/2$ provided that the critical points of f lie in the sector $\{re^{i\theta}: r > 0, |\theta| \leq \pi/6\}$, and $|f(\zeta)/\zeta| < 2/3$ if they lie in the union of the two rays $\{1+re^{\pm i\theta}: r \geq 0\}$, where $0 < \theta \leq \pi/2$. Copyright © 2010 Australian Mathematical Publishing Association Inc.

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Keywords

Critical points, Polynomials, Smales problem